Ocular Biomechanics and Biotransport

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■ **Abstract**   The eye transduces light, and we usually do not think of it as a biomechanical structure. Yet it is actually a pressurized, thick-walled shell that has an internal and external musculature, a remarkably complex internal vascular system, dedicated fluid production and drainage tissues, and a variety of specialized fluid and solute transport systems. Biomechanics is particularly involved in accommodation (focusing near and far), as well as in common disorders such as glaucoma, macular degeneration, myopia, and presbyopia. In this review, we give a (necessarily brief) overview of many of the interesting biomechanical aspects of the eye, concluding with a list of open problems.

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INTRODUCTION

The eye is a remarkable organ, specialized for the conversion of photons into spatially organized and temporally resolved electrochemical signals. Biomechanics plays a major role in the normal and pathological function of the eye. We begin with a brief anatomical review of some of the biomechanically important parts of the eye.

Overview of Ocular Anatomy

The outer envelope of the eye is formed by two connective tissues, the cornea and sclera (Figure 1). Six extraocular muscles attach to the outer sclera, acting to rotate the eye in concert with a clever system of active pulleys (1). The corneoscleral envelope forms a closed shell, pierced at the back of the eye by the scleral canal and at other discrete locations by small vessels and nerves. The optic nerve, responsible for carrying information from the retina to the visual center in the brain, leaves the eye through the scleral canal. Light enters the eye by passing through the cornea, after which it traverses the anterior chamber, pupil, lens, and vitreous body before striking the retina. The lens is suspended by ligaments (the zonules) that attach to the inner fibers of the ciliary muscle; alterations in tone of these muscle fibers cause the zonules to tug on the lens, so that the lens changes shape to alter the focal length of the eye in a process known as accommodation.

The ciliary body consists of the ciliary muscle and a highly folded and vascularized inner layer known as the ciliary processes, which secrete a clear, colourless fluid called the aqueous humor. This fluid flows radially inward, bathing the lens, then flows anteriorly through the pupil to fill the anterior chamber and nourish the cornea, before draining out of the eye through specialized tissues in the angle formed by the iris and cornea. As we will see, this fluid flow is responsible for creating a positive pressure within the eye, the so-called intraocular pressure (IOP), which has many interesting biomechanical consequences. Additionally, the volume of vascular beds within the eye changes throughout the cardiac cycle, creating a time-varying component of the IOP in an effect known as the ocular pulse. The space behind the lens is filled with a relatively inert connective tissue called the vitreous body. It is quite porous and thus transmits the pressure from the anterior chamber throughout the interior of the eye.

OCULAR BIOSOLID MECHANICS

The eye is subjected to a mean and time-varying internal pressure; furthermore, the ciliary muscle can create significant internal forces, whereas the extraocular muscles create external forces. Despite these forces, the eye must maintain the proper relative positions of all optical components so as to ensure high visual acuity. This leads to some interesting biosolid mechanics.

Mechanics of the Sclera and Corneoscleral Envelope

The corneoscleral shell encloses the intraocular tissues and protects the eye from blunt injury. It is a surprisingly tough tissue that has a high elastic modulus and a very high rupture strength. Measurements on intact inflated human ocular globes have yielded average Young's moduli in the range of 5–13 MPa (3–5). The sclera is largely composed of circumferentially oriented types I and III collagen fibers and thus has a modulus in the circumferential direction much higher than in the radial (6).

Knowledge of the elastic properties of the sclera is important in several applications: improving the accuracy of methods to measure IOP and resistance to aqueous humor drainage, understanding the development of myopia (near-sightedness), and interpreting the magnitude of the ocular pulse. We first review the many studies done to measure mechanical properties of the sclera and to model the stress-strain behavior of the corneoscleral envelope. Then we examine the application of these findings.

Friedenwald (7) first proposed the "ocular rigidity function," describing the change in intraocular pressure, ($IOP–IOP_0$), with a change in ocular volume, ($V - V_0$):

$$\ln\left[\frac{IOP}{IOP_0}\right] = K(V - V_0), \tag{1}$$

where K is the coefficient of ocular rigidity. In humans, K is approximately 0.05 μl^{-1} (8), giving a compliance of the ocular envelope of roughly 1 μl/mmHg at a physiologic IOP of 15 mmHg; the bovine eye is considerably less stiff with an ocular rigidity that is roughly tenfold smaller.

Equation 1 is consistent with the mechanical properties of collagen, which is responsible for the high elastic modulus of the sclera. Specifically, collagen exhibits a stress (σ)/strain (ε) relationship of the form (9)

$$\sigma = A[e^{\alpha\varepsilon} - 1], \tag{2}$$

where A and α are material constants. Note that at low strains, Aα is equivalent to the Young's modulus of the material.

The tangential (hoop) stress in the sclera can be related to the intraocular pressure using Laplace's relation: $\sigma = IOP\, R/(2h)$, where R is the radius of the eye and h is the thickness of the sclera. Considering small strains, such that $\varepsilon = (R - R_0)/R_0$ (but not so small that Equation 2 is linear), we let $V - V_0 = 4\pi\, R_0^2\, (R - R_0)$. Approximating Equation 2 as $\sigma = A \exp(\alpha\,\varepsilon)$, Equation 1 results. The approximation is reasonable when strains are large enough that the nonlinear term dominates Equation 2, which occurs for very small strains indeed because α is very large. Keeping the full form of Equation 2 leads to a modified form of the

Friedenwald equation (in the small strain limit):

$$\ln \left[\frac{IOP + \dfrac{2hA}{R}}{IOP_0 + \dfrac{2hA}{R}} \right] = \frac{\alpha}{V_0}(V - V_0). \tag{3}$$

McEwen & St. Helen (10) first introduced Equation 3, and Collins & Van der Werff (8) summarized their results for human eyes to obtain $\alpha/V_0 = 0.022\ \mu l^{-1}$ and $2hA/R = 9.5$ mmHg. If we let the typical radius and thickness of the human corneoscleral shell be 1.15 cm and 0.06 cm, respectively (8), then $\alpha = 140$ and the low strain modulus, $A\alpha$, is 1.7 MPa. Greene derives Equation 3 more rigorously and reviews the literature to give a range of values for α, A, and the compliance of the eye (11).

Note that the ocular rigidity function really characterizes the properties of both the sclera and the cornea. Although the cornea is somewhat less stiff than the sclera (12–14), its elastic properties can also be described by a relationship analogous to Equation 2. Thus, Equation 3 actually describes the behavior of the corneoscleral envelope.

These formulations treat the sclera and cornea as elastic materials, but the ocular envelope also shows time-dependent deformations upon the application of stress. Viscoelastic models have been used to characterize this behavior (15–17), but, as in other tissues, a variety of time-constants are necessary to capture the behavior. This is likely due to the fact that the sclera is a biphasic material and thus better characterized by models that allow coupling of stresses with fluid motions in or out of the tissue (18, 19).

APPLICATIONS OF SCLERAL MECHANICS The most common use of the Friedenwald relationship is for tonometry (noninvasive measurement of IOP). There are different types of tonometers (20), the conceptually simplest of which is the Schiotz tonometer. This device measures the depth of indentation that occurs when a plunger of known weight is placed against the cornea. Gloster (21) summarized data for the relationship between intraocular pressure and the scale reading (for a given tonometer weight). However, this is the pressure in the eye with the tonometer distorting the eye. What is desired is the pressure of the undeformed eye. The indentation of the eye is equivalent to the injection of a fluid volume into the eye equal to the indentation volume. Gloster found a relationship between indentation depth and indentation volume of the tonometer. Then, using the Friedenwald relationship (Equation 1), the undeformed IOP can be found (22). This requires knowledge of the ocular rigidity, found either by using a population average or by using the Schiotz tonometer with two different plunger weights (22).

A related application of the Friedenwald relationship is in tonography in which a modified tonometer is used to estimate the aqueous humor drainage resistance in a live eye (23) (see also Aqueous Humor Dynamics, below). After the plunger increases the pressure in the eye, the pressure slowly decays as this indentation

volume flows out via the aqueous humor drainage pathway. By measuring the change in pressure over a short period of time (Δt, usually 4 min.), Equation 1 can be used to calculate the volume decrease of the corneoscleral envelope during this period (ΔV_s). Additionally, because the plunger indentation into the cornea increases as the pressure in the eye drops, this increased indentation volume (ΔV_c) must be included in the estimate of the total volume that has passed out of the eye. Then, outflow facility, C, the inverse of aqueous drainage resistance, can be estimated as $C = (\Delta V_s + \Delta V_c)/(\Delta t \, \Delta P)$, where ΔP is the average increase in IOP that occurred during the tonography. Greene (11) emphasized that ocular rigidity should be determined for a given eye before performing tonography, as very different results are expected for eyes of differing volumes (compare Equations 1 and 3 to see that K is inversely proportional to ocular volume). Note also that viscoelastic creep might confound the measurement of outflow facility by this method, but experimental studies indicate that this is not a serious error (24, 25).

Another important application of scleral mechanics is the understanding of myopia in which the axial length of the eye is too large to allow clear focussing of distant light rays on the retina. So far, we have considered the sclera to be a nonlinear elastic or viscoelastic material; however, the sclera has an elastic limit beyond which plastic deformation occurs (26, 27). Among the mechanical theories for explaining myopia, it has been postulated that these young eyes have (*a*) a genetically inherited decrease of this elastic limit, (*b*) higher than normal stresses on the sclera associated with accommodation and convergence that occur when reading (28), or (*c*) stretching caused by periodic increases in IOP owing to squinting or eye rubbing (27). It is possible that one or more of these mechanisms, combined with the physiological feedback loop responsible for growth of the eye (29–31), leads to the development of myopia.

Corneal Biomechanics

The cornea is a multilaminate tissue, consisting of an anterior stratified squamous "tight" epithelium ($\sim$50 microns thick), a tough collagenous stroma, and a posterior "leaky" monolayer of actively pumping endothelial cells ($\sim$5 microns thick). Its combination of remarkable strength and transparency is due to the highly organized micro- and nanoscale structure of the stroma (32, 33). On the microscale, the stroma comprises a nematic stack of 250–400 lamellae (34) containing type I/V heterotypic collagen fibrils (35). These fibrils run preferentially in the meridonal, horizontal, and (in the periphery) circumferential directions (36), and together help bear the load imposed by the IOP (Figure 2). In fact, the load may be taken up in a complex manner both in the plane of the cornea and transversely (37–40). Remarkably, there is no consensus on how the cornea is loaded in vivo. On the nanoscale, hydrophilic proteoglycans surround the 35-nm monodisperse collagen fibrils and impose a relatively uniform spacing on the collagen. The cornea's transverse material properties are determined primarily by the 36–48 mM of fixed charge density associated with the presence of these organizing proteoglycans (41, 42).
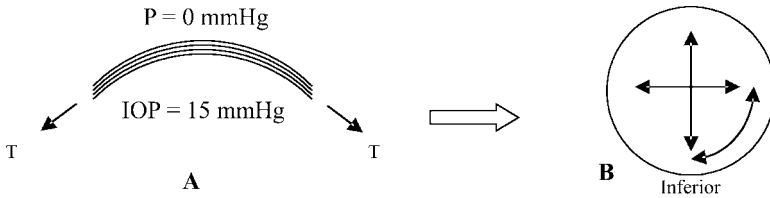
Figure 2   Corneal tensile load bearing. (*A*) Transverse view of cornea. Conversion of the 15 mmHg pressure difference across the cornea results in a tangential tensile force that is carried by the stromal lamellae. (*B*) En face view of cornea. Lamellar fibrils are thought to be oriented in three preferential orientations, which explains the anisotropic nature of the measured tensile modulus in the stroma.

MATERIAL PROPERTIES   To generate a nearly perfectly spherical, aberration-free surface, the cornea must distribute applied loads with remarkable precision. To effect predictable shape changes to correct refractive errors, the corneal response to tissue resection/ablation must be characterized. Thus, it is of interest to discern the material properties of the cornea, which are heterogeneous, highly anisotropic, nonlinear, and viscoelastic. For example, for meridonal loading at normal IOP, Young's secant modulus is largest in the central cornea (8.6 MPa), whereas for circumferential loading, the secant modulus is largest in the periphery (13.0 MPa) (5). Woo et al. (4) used finite element analysis to obtain a nonlinear effective stress-strain relationship for clamped inflated human corneas of the form of Equation 2 with $A = 5.4 \times 10^4$ dyne/cm^2 and $\alpha = 28.0$. A more recent study of 12 human corneas found $A = 1.75 \times 10^4$ dyne/cm^2 and $\alpha = 48.3$ (43). Stress relaxation curves demonstrating the viscoelastic nature of peripheral corneal strips were fit with the following empirical equation (44):

$$y = -0.0159 \ln(t) + 0.9785, \tag{4}$$

where y is the normalized storage modulus at a fixed stretch ratio of 1.5 and t is time in seconds.

SWELLING PRESSURE   In the anterior-posterior direction, the mammalian corneal stroma lacks internal mechanical constraints. The stroma therefore has a tendency to imbibe water, which is quantified through its "swelling pressure" (45). To prevent swelling, which leads to opacity, the cornea is compressed by the combined action of its limiting membranes (46), as discussed in detail in Transport Within the Cornea, below. Therefore, it is of interest to understand the magnitude and nature of the swelling forces that must be controlled to preserve vision. Stromal swelling pressure depends strongly on hydration (Figure 3), and can be described by (47)

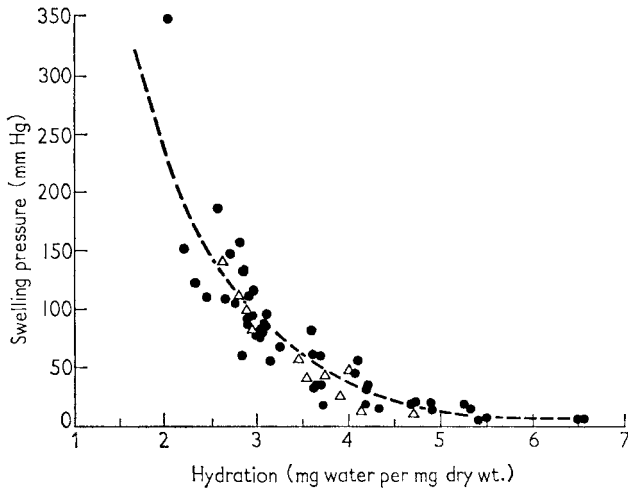$$p = \gamma \exp(-\beta H), \tag{5}$$

Figure 3   Swelling pressure in rabbit (*filled circles*) and human (*open triangles*) corneal stroma versus stromal hydration (mass water/mass dry tissue). The broken curve represents steer swelling pressure. At normal hydration (3.2–3.4 mg H_2O/mg dry material), this stromal swelling pressure is approximately 60 mmHg (52). From Hedbys & Dohlman (53).

where p is swelling pressure, γ and β are constants, and H is the hydration of the stromal tissue. Equation 5 is a regression of experimental data and tells us little about the physics of stromal swelling forces. Taking a more fundamental physical approach, Eisenberg & Grodzinsky (48, 49) extended KLM (50, 51) biphasic theory to include the effects of ionic species, expressing the swelling stress in the stroma, σ, as a function of the strain, ε, and the concentration of ionic species, c:

$$\sigma(c, \varepsilon) = E_A(c)\varepsilon + \sigma_c(c), \tag{6}$$

where E_A is the aggregate modulus [sum of the Lame's constants—$2G(c) + \lambda(c)$] and σ_c is the chemical stress. Eisenberg & Grodzinsky were able to extract both E_A and $\sigma_c(c)$ as functions of c and use Equation 6 to predict the free swelling of the corneal stroma with reasonable accuracy (48).

APPLICATION TO REFRACTIVE SURGERY   An obvious application of corneal biomechanics is to predict the laser ablation profile that will optimize postoperative visual acuity in refractive corneal procedures. However, biomechanical modeling has not been particularly successful in this task. Instead, laser manufacturers depend on continually updated, proprietary empirical algorithms (54) based on direct shape-subtraction (55) formulas that have been modified and statistically optimized to the mean patient population postoperative response (54). This empirical approach has been quite successful with up to 97% of the subjects willing to recommend LASIK (Laser ASsisted In-situ Keratomileusis) to a friend (56). How, then, did

the biomechanician fail, with the embarrassing result that human corneas became test cases for the development of a vast empirical database?

In spite of a sophisticated effort to model radial keratotomy (RK) refractive surgical outcomes during the late 1980s and early 1990s (57–61), the practical application of these models never really gained acceptance for four reasons: (*a*) Early RK models could not be validated (61); (*b*) the spatially variant mechanical properties of the stroma are not well defined on the relevant microscopic length scale (37); (*c*) the distribution of load in the stroma, which sets the local value of the nonlinear tensile modulus [to which refractive models are highly sensitive (43)] is not definitively known; and finally (*d*) the long-term stromal remodeling response is not addressed at all by mechanical models. These limitations, in combination with the undeniable effectiveness of the empirical approach, have virtually ensured that predictive biomechanical modeling of refractive procedures is not likely to enjoy resurgent popularity in the near future. In a further ironic twist, topographic corneal maps obtained following laser ablation surgeries are being used to "back out" information about stromal structure and material properties (54).

Retina and Lamina Cribrosa Biomechanics

The retina is a remarkably fragile tissue, having a thickness of 250 μm (62) and a Young's modulus of only 20 kPa (63). It does not carry significant load, but it can tear, usually with drastic visual consequences. Retinal tears are often associated with age-related liquefaction and shrinkage of the vitreous body (64), but can also occur when the eye is subjected to large accelerations (65), such as in shaken baby syndrome (66).

The lamina cribrosa is one of the most biomechanically interesting tissues in the eye. It is a porous connective tissue that spans the scleral canal, mechanically supporting the retinal ganglion cells of the optic nerve as they pass through the scleral canal. The lamina cribrosa is very important in glaucoma, a group of diseases having a common clinical end point of visual field loss and characteristic changes to the optic nerve. Glaucoma is the second most common cause of blindness in western countries and afflicts approximately 65 to 70 million people worldwide (67). In the most common forms of glaucoma, IOP is elevated (to 21 mmHg or higher), and if this elevated IOP is sustained, retinal ganglion cell loss ensues and blindness eventually results. We do not yet completely understand the mechanism of ganglion cell loss, but studies have strongly suggested that the lamina cribrosa is the site of damage (68–70). This has led to the mechanical theory of glaucomatous optic neuropathy, which postulates that elevated mechanical stresses acting within the lamina cribrosa lead to nerve fiber damage, probably through activation of Type 1-β astrocytes and/or other glial cells (71). Such mechanical effects may combine synergistically with altered vascular perfusion in the optic nerve head to damage retinal ganglion cells (see Blood Flow in the Eye, below).

In order to evaluate the possible role of mechanical stress in glaucoma, we must know something about the mechanical environment within the lamina cribrosa. Unfortunately, the lamina cribrosa is small, relatively inaccessible, soft, and

surrounded by a much stiffer tissue (sclera). This makes experiments challenging, and most measurements have relied on post mortem histologic examination (72, 73), or other indirect measurements of deformation (74–76). Others have adopted a modeling approach, treating the lamina as a circular plate of finite thickness (77, 78). Unfortunately, the lamina is much more geometrically complex than such analytic treatments allow, and thus numerical modeling is an attractive option. Bellezza et al. (79) considered a simplified model of the lamina cribrosa consisting of regular networks of connective tissue "bridges" spanning an elliptical scleral canal. Their results showed remarkable stress elevations in the lamina cribrosa bridges, in some cases more than 100 times the applied IOP. Sigal et al. (80), also using a finite element approach, modeled the sclera, lamina cribrosa, and pre- and postlaminar nerve tissue, finding von Mises strains of up to 12% within the lamina at an IOP of 50 mmHg. Such models are relatively crude at present, assuming linear elasticity, tissue isotropy, and simplified geometries. Nonetheless, when supported by suitable experimental studies, they are a promising tool for unraveling the mysteries of lamina cribrosa biomechanics in glaucoma.

Accommodation and Presbyopia

Although there are many changes that occur with aging, perhaps the most universal is the loss of the ability to accommodate, i.e., to change the focal length of the eye by changing lens shape. This condition is known as presbyopia, familiar to everyone who has purchased a pair of reading glasses, and typically begins during the fifth decade of life. Several hypotheses have been offered for the causes of presbyopia, including (*a*) a decreased elasticity of the lens, making it more resistant to deformation; (*b*) changes in the geometry of the anterior segment and the lens, resulting in a loss of mechanical effectiveness of zonular tightening; and (*c*) loss of ciliary muscle contractility.

There appears to be good evidence supporting all of these hypotheses. The lens definitely becomes stiffer with age (81–83). There are changes in the geometry of the anterior segment, including an anterior motion of the lens and of the ciliary muscle, an increased size and curvature of the lens, and a decreased anterior chamber depth (84). Other studies (85, 86) have shown that although the ciliary muscle loses its ability to contract in older individuals, the muscle itself is not weakened (87, 88) and remains sensitive to cholinergic agonists (89). Recent evidence indicates that changes in the connective tissues around the ciliary muscle may inhibit its ability to freely contract (90). Thus, the pathophysiology of presbyopia may be multifactorial.

OCULAR BIOFLUID MECHANICS AND TRANSPORT

Blood flows through the eye, aqueous humor is produced within and drains from the eye, and interstitial fluid percolates through connective tissues within the eye. These myriad fluid pathways contain many fascinating and challenging biomechanical problems.

Blood Flow in the Eye

All blood is supplied to the eye by the ophthalmic artery. The eye has two main vascular systems: the retinal and uveal. The retinal circulation is fed and drained by the central retinal artery and vein, both of which enter the eye through the scleral canal. The retinal circulation is responsible for supplying blood to the inner retina and is autoregulated (91, 92) so that it provides a nearly constant blood flow rate even as IOP increases up to 30 mmHg. Above this pressure, blood flow is reduced as IOP increases. As the blood flow to the inner aspects of the optic nerve head is also served by the retinal circulation (91), this may have some importance in glaucoma.

The uveal circulation can itself be divided into two parts. The anterior uveal circulation is responsible for supplying blood to vascular tissues of the anterior eye, in particular the iris and ciliary body, where it is involved in the formation of the aqueous humor (see Aqueous Humor Dynamics, below). The iridial circulation is autoregulated (91). The posterior uveal circulation feeds a specialized vascular bed known as the choroid, lying between the retina and sclera. The choroid supplies blood to the outer retina, which has a very high metabolic rate (93). In fact, the choroidal flow is the highest flow per perfused volume of any tissue in the body (8), with approximately 85% of total ocular blood flow passing through the choroid (91). Because the oxygen needs of even the retina are greatly exceeded by this supply (91), the reason for such a high perfusion rate is not known, although a number of creative hypotheses have been offered (94–97). The choroidal flow is thought not to be autoregulated (91), but there is some recent evidence to the contrary (98, 99). The uveal circulation is drained by a venous system consisting of two parts (100). Most blood drains through the vortex veins, four large veins (in the human) that exit the eye through the posterior sclera. The anterior ciliary veins drain part of the ciliary muscle.

The physiology of blood flow in the eye, particularly on the venous side, is strongly influenced by IOP. In most of the circulatory system, flow is determined by the difference between the arterial and venous pressures. However, in the eye, the perfusion pressure is the difference between the arterial pressure and IOP. This relates to the well-known problem of flow through collapsible tubes under the influence of an external pressure (101–103). When the external pressure surrounding a blood vessel is greater than the pressure within that vessel, the vessel collapses, initially at the distal end of the vessel, where the pressure is lowest. As this constriction is the location where most of the pressure drop occurs, upstream of this collapse region the pressure in the vessel is at least equal to the external pressure. Thus, while the arterial pressure in the eye is somewhat lower than in the rest of the body [in the uvea, 75 mmHg systolic and 35 mmHg diastolic (104)], venous pressure in the eye (other than in the sclera) is always above 15 mmHg. Pressures in the choriocapillaris are typically 5–10 mmHg higher than IOP (100).

The region of vessel collapse occurs in the veins as they pass from the vitreous chamber into the sclera. This collapse is necessary for the pressure in the vessel to drop from IOP to episcleral venous pressure [typically 8–10 mmHg in the eye (105,

106)]. The dramatic change in the vessel cross-section that occurs at this point is known as a vascular waterfall. It is a point of flow limitation, similar to what occurs at the nozzle throat in supersonic flow, or at a waterfall (102). In all of these flows, once the flow velocity has reached the wave speed at the point of flow limitation, the flow becomes insensitive to the downstream pressure. The consequence is that, as indicated above, ocular blood flow is very sensitive to the IOP. This is likely the reason why several of the circulations in the eye are autoregulated. It is also the basis for the theory that glaucomatous damage to the optic nerve is caused by reduced blood flow owing to the elevated IOP (107).

Aqueous Humor Dynamics

For proper visual acuity the eye must be relatively rigid, yet the mammalian eye contains no bones. How then is rigidity maintained? Further, the lens and cornea must remain clear to allow light transmission, and therefore cannot be invested with a vasculature. How then are the cells nourished in these tissues? The eye has solved both problems with a common (and clever) mechanism: The corneoscleral shell is inflated by the production and drainage of the aqueous humor, which also serves to nourish the lens and cornea. The best analogy is a soccer ball with a slow leak whose air is constantly being replenished from a pump. The aqueous humor can also clear debris from within the eye, e.g., red cells from intraocular haemorrhage.

The aqueous humor is produced at 2.4 ± 0.6 μl/min (mean $\pm$ SD, daytime measurements in adults aged 20–83 years) (108). This corresponds to a turnover rate of 1% of the anterior chamber volume per minute, i.e., relatively slowly. Aqueous humor production varies diurnally: It is normally about 3.0 μl/min in the morning, 2.4 μl/min in the afternoon, and drops to 1.5 μl/min at night (108). It is produced primarily by active transport across epithelial cells lining the surface of the ciliary processes (109), and the rate of production is relatively independent of IOP.

The aqueous humor drains from the eye via two routes, the so-called conventional and uveo-scleral (or unconventional) routes. Uveo-scleral outflow normally carries only approximately 10% of total outflow (110, 111); we consider it again in Scleral Permeability and Drug Delivery to the Eye, below. Most aqueous humor instead drains via specialized tissues situated in the angle of the anterior chamber, located at the conjunction of the iris, cornea, and sclera. Beginning at the anterior chamber and moving exteriorly, these tissues are the trabecular meshwork, a porous connective tissue; Schlemm's canal, a collecting duct lined by a vascular-like endothelium; and the collector channels/aqueous veins. Direct pressure measurements (112, 113) and circumstantial evidence (114) indicate that most of the flow resistance in the normal nonglaucomatous eye is in the juxtacanalicular tissue (JCT) or the endothelial lining of Schlemm's canal. After leaving the aqueous veins, the aqueous humor mixes with blood in the episcleral veins, eventually draining back to the right heart (Figure 4). The episcleral venous pressure is approximately 8–10 mmHg (105, 106), and the resistance of the

conventional aqueous drainage tissues is approximately 3–4 mmHg/μl/min, resulting in an IOP of 15.5 $\pm$ 2.6 mmHg (mean $\pm$ SD) in the general population (115).

This would be an interesting curiosity if it were not for the problem of glaucoma. We know that elevated IOP is the main risk factor for glaucoma, and that lowering IOP helps preserve visual function (116). In the vast majority of glaucomas, the elevation in IOP is due to too much aqueous humor drainage resistance, and in the majority of these cases the elevated resistance is due to pathologic changes in the conventional drainage tissues. Despite years of intensive research, we understand little of how aqueous drainage resistance is controlled in normal and glaucomatous eyes.

One of the big questions in glaucoma research is: Where is the aqueous flow resistance? Models of Schlemm's canal as a compliant chamber with a porous, elastic wall suggest negligible flow resistance within the canal itself, except at extreme intraocular pressures (>50 mmHg) when the canal collapses (117). Known concentrations of proteoglycan-rich gels within the extracellular spaces of the juxtacanalicular tissue are consistent with the generation of significant flow resistance (118); recent data suggest that the turnover of this matrix is modulated by stretch-induced matrix metalloproteinases (MMP) activity within the trabecular meshwork (119–121). However, the evidence supporting a primary role for extracellular matrix is far from iron-clad (see review in 122), and researchers have looked elsewhere. The other "candidate" for generating flow resistance is the endothelial lining of Schlemm's canal. This cellular layer is unusual; for example, it has the highest permeability of any endothelium (123), with $L_p \geq 4 \times 10^{-8}$ cm^2 s/g, yet it is nonfenestrated (but see below). The cells are joined by tight junctions that become less tight as IOP increases (124) and are permeated by membrane-lined openings (pores) that, although poorly understood, are almost certainly involved in aqueous humor transport (125). The pores represent only approximately 0.1% of the total endothelial area and have a mean diameter just slightly over 1 μm (125). A model of the pores in the endothelial lining modulating the flow through a porous juxtacanalicular tissue (127) suggests that overall flow resistance may depend on an interaction between the endothelial pores and extracellular matrix.

The endothelial cells lining Schlemm's canal bulge prominently into the lumen of the canal, forming the so-called giant vacuoles. Evidence suggests these are passive structures that form in response to the "backward" basal-to-apical pressure gradient that is always present across the cells (128, 129). The extreme case is when you rub your eyes, instantaneously generating pressures as high as 80 mmHg (130)! These large IOPs form so many giant vacuoles that inner wall endothelial cells may stretch by as much as 50% (131), a harsh biomechanical environment indeed.

The biomechanics of aqueous humor flow within the anterior chamber are also interesting. Because the cornea is normally exposed to ambient air, the temperature at the posterior corneal surface is slightly less than body temperature, thus creating a temperature gradient across the anterior chamber. The resulting convection patterns (132, 133) tend to transport particles in vertical paths along the mid-peripheral

cornea (Figure 4). The clinical correlate of this effect is pigment particles that are seen to accumulate along such paths in patients whose irises release abnormal amounts of pigments.

There is a form of glaucoma in which the elevated IOP is not due to changes in the drainage system of the eye per se. This is angle-closure glaucoma, when the iris pivots forward and blocks access to the drainage structures in the angle of the anterior chamber. There appears to be an anatomic predisposition to this situation. The iris is extremely pliable (134), and modeling has shown interesting interactions between iris deformation and aqueous flow through the pupil and between the lens and the iris, especially when the eye is perturbed by blinking (135, 136).

Transport Within the Cornea

To maintain transparency, the corneal stroma must be prevented from swelling. The flows and forces that nourish and deturgesce the stroma are subtle and complex. Although there is some evidence for limbally derived lateral flow (137, 138) because of the 10:1 ratio of lateral to transverse diffusion distance, the corneal transport system is essentially one-dimensional in the AP (anterior-to-posterior) direction (Figure 5). To understand this AP transport, we must consider the role of the corneal membranes. The epithelium, with its complete tight junctions, primarily protects the stroma [although it does have some limited active pumping ability (139)], whereas the endothelium, with its incomplete tight junctions and its plethora of basolateral ATPases, removes fluid yet allows free diffusion of nutrients and cytokines from the aqueous humor (46). Globally, there is approximately a 20 micron/h net flow velocity out of the cornea to the tear film, driven by the transcorneal pressure gradient and by evaporation from the tear film (140). Intriguingly, however, the corneal endothelium can generate a fluid velocity of 40 microns/h in the opposite direction, effectively compressing the stroma (141).

Fluid transport through the cornea depends on the hydraulic permeabilities, L_p, of the endothelium, epithelium, and stroma. Isolating functioning membranes from
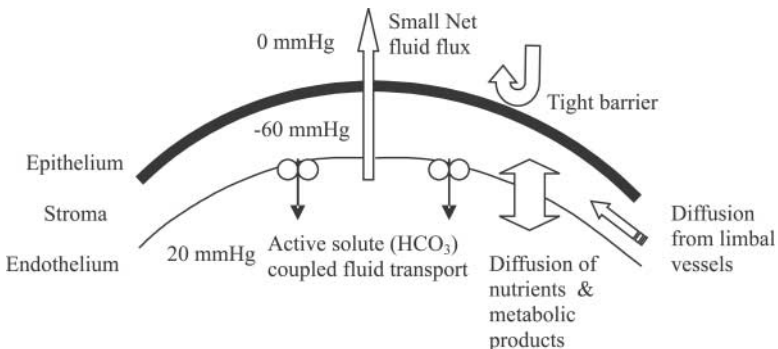

Figure 5   Key elements of the corneal transport system.

the hydrophilic stroma to measure L_p is not feasible. However, Klyce & Russell (142) were able to extract L_p for both the endothelium (42.0×10^{-12} cm^3/dyne sec) and the epithelium (6.1×10^{-12} cm^3/dyne sec) by coupling thermodynamic representations of the membranes (143) to a dynamic stromal transport model (47) and fitting the model to the corneal response to osmotic challenges. As expected, the endothelium is more permeable to water than the epithelium (by a factor of seven). From the same series of experiments, the ratio of endothelial to epithelial NaCl permeability was much larger than one as well. To produce dynamic corneal transport models (e.g., 142), it is necessary to know the value of stromal hydraulic conductivity, k/η, as a function of tissue hydration. The elegant work of Hedbys & Mishima (144) relates the stromal hydraulic conductivity in both the in-plane and transverse direction to hydration (Figure 6).

Typically, stromal fluid transport and hydraulic conductivity have been measured on bulk tissue. Recently, however, Ruberti et al. (145) tracked microscale
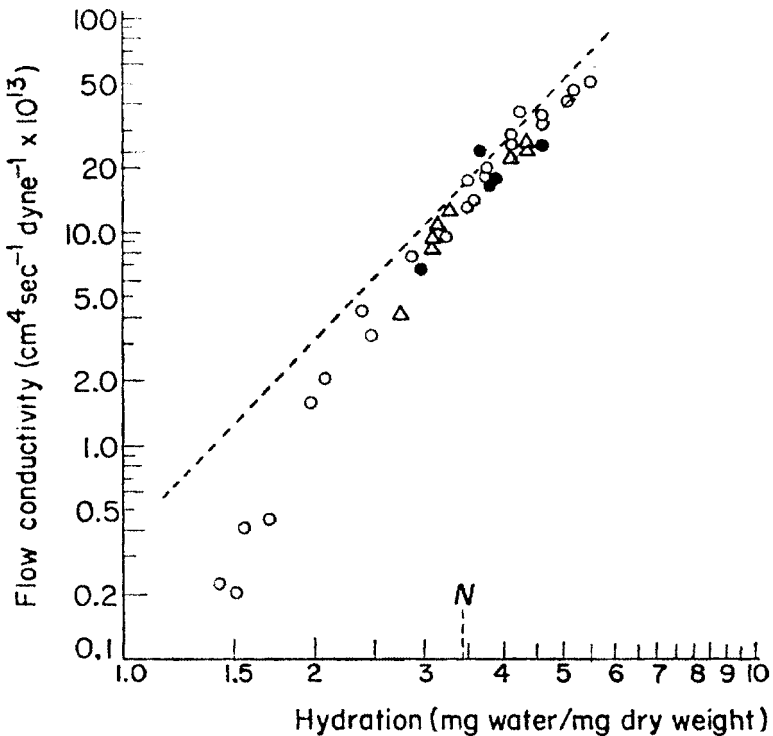

Figure 6 Flow conductivity versus hydration across the cornea. The symbols refer to measurements taken with (*closed circles*) and without (*open circles*) Descemet's membrane in 0.9% NaCl, or without Descemet's membrane in distilled water (*triangles*). The broken line represents the flow conductivity versus hydration relationship for flow along the cornea. N is the normal corneal hydration. From Hedbys & Mishima (144).

intrastromal flows in response to corneal debridement, and Overby et al. (146) determined intrastromal specific hydraulic conductivity directly from structure-preserving micrographs. Such investigations promise to improve our understanding of microscale corneal transport dynamics.

Transport Across Bruch's Membrane

In addition to the corneal endothelium, there are several sites of active transport in the eye, including the ciliary epithelium, responsible for production of aqueous humor, and the retinal pigment epithelium (RPE), which removes fluid from the retina and thus helps keep the retina attached (147–149).

The RPE rests on a basement membrane that is part of Bruch's membrane, a five-layer barrier structure that limits transport between the choroid and the outer retina. These five layers, beginning at the RPE and proceeding outward toward the choroid, are the basement membrane of the RPE, the inner collagenous layer, the elastin layer, the outer collagenous layer, and the basement membrane of the choriocapillaris (150). Oxygen, electrolytes, nutrients, and cytokines from the choroidal circulation must pass through this barrier to reach the retina, whereas waste products from the retina and water pumped by the RPE must pass back through this barrier to be eliminated into the blood stream.

Water transport through this membrane is the best studied of these transport processes. After the RPE pumps water from the retinal space into Bruch's membrane, the water moves under the influence of both hydrostatic and osmotic pressure gradients into the choroidal circulation (91, 151). The hydraulic resistance of Bruch's membrane increases with age (Figure 7). This increase has been hypothesized to contribute to the pathology of age-related macular degeneration (AMD) by inhibiting fluid transport by the RPE and consequently causing retinal detachment (152).

The age-related increase in the hydraulic resistance of Bruch's membrane is thought to be a consequence of lipid accumulation (153) because the age-related increase in resistance parallels the age-related accumulation of lipid in Bruch's membrane (Figure 7). These lipids may originate as waste products from the retina that are processed by the RPE (154).

It has been shown that there is a parallel age-related increase in the transport resistance of Bruch's membrane to protein transport (156), although that study may not have properly accounted for osmotic effects of the proteins examined. Little study has yet been done on the transport of other moieties across Bruch's membrane.

Scleral Permeability and Drug Delivery to the Eye

Drug delivery to intraocular tissues is important in treating a variety of ocular diseases. Systemic administration of these agents is undesirable because it necessitates high plasma concentrations to achieve adequate intraocular dosing. Transcorneal delivery by passive diffusion is difficult because the drug needs to have
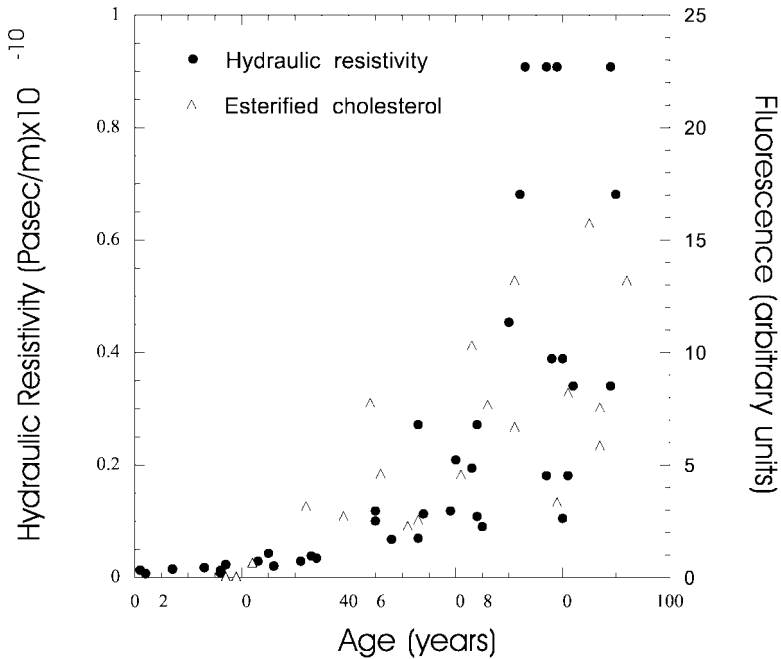
Figure 7   Hydraulic resistivity (150) of excised Bruch's membrane/choroid (*closed symbols*) and fluorescence owing to histochemically detected esterified cholesterol in sections of normal Bruch's membrane (155) (*open symbols*) as a function of age.

hydrophobic characteristics to pass through the corneal epithelium and endothelium, and hydrophilic characteristics to pass through the corneal stroma. Furthermore, as soon as the agent enters the anterior chamber, it is carried out of the eye by the aqueous humor. Scleral delivery, especially for drugs destined for the retina (157), may be a more attractive route for drug administration (158), as the tight epithelial barriers of the cornea are not present on the sclera (159). However, the scleral stroma is still a significant barrier, and a number of studies have examined the permeability of this tissue.

As expected, scleral permeability to solute transport decreases with increasing solute molecular weight and increasing molecular radius, with the latter a better predictor of scleral permeability than the former (160). The posterior sclera is more permeable to solute transport than the anterior sclera, further supporting the sclera as an ideal route for drug delivery to the retina (161).

The specific hydraulic conductivity of the sclera is 2×10^{-14} cm^2, typical of dense connective tissues (162). With a typical pressure difference across the sclera of 15 mmHg; a scleral thickness, L, of 0.6 mm (163); and a filtering area, A, of 11.5 cm^2 [the total scleral area (163)], we can use Darcy's law to estimate a

maximum flow rate (Q) across the sclera of 0.3 μl/min. The flow rate can be used to examine several issues related to fluid flow though the scleral stroma.

The first question is the extent to which this flow impedes drug delivery across the sclera. The diffusional flux of a drug through a tissue can be estimated as

$$D_0(1 - \Phi)A\frac{\Delta C}{L}, \tag{7}$$

whereas the convective flux of a drug through that same tissue would be

$$QC(1 - \Phi). \tag{8}$$

Here D_0 is the diffusion coefficient of the tracer in free solution (for albumin 6×10^{-7} cm^2/sec); Φ is the extent to which the tracer is retarded, relative to the fluid flow, from moving by the extracellular matrix (0 is unhindered, 1 completely hindered); and ΔC is the concentration difference across the sclera, which we assume is the same as the concentration of drug at the surface of the sclera. Using these formulas, the ratio of diffusional transport to convective transport is computed to be approximately 20 for molecules the size of albumin. In other words, for these parameters, diffusional transport of a drug across the sclera is more than an order-of-magnitude higher than transport of the drug by convection. Thus, bulk flow across the sclera should have minimal impact on drug delivery through the sclera.

We can also use the value of Q to gain insight into the unconventional drainage pathway (Aqueous Humor Dynamics, above) that normally carries a small fraction of the aqueous humor from the eye. Aqueous humor draining via this pathway passes through the ciliary muscle, into the suprachoroidal space, and then passes (*a*) either through the sclera into the orbit or (*b*) through the sclera to the vortex veins and choroidal circulation, where it is absorbed. Arguments have been provided for each of these pathways (123, 164, 165). The value of Q calculated above as 0.3 μl/min would appear to support the former pathway because this value is consistent with measured values of unconventional aqueous outflow rates (166). However, it is known that ciliary muscle contraction greatly affects the unconventional outflow (167), and that PGF$_{2\alpha}$ greatly increases unconventional outflow by decreasing the flow resistance of the interstitial spaces in the ciliary muscle (168, 169). This can only be the case if the flow resistance of the ciliary muscle is of the same order of magnitude or even larger than that of the sclera; otherwise, changes in the muscle would make little difference. But, in that case, the calculated flow rate of 0.3 μl/min must be an upper bound that does not consider the flow resistance of the ciliary muscle. A further argument against a trans-scleral flow is that unconventional outflow is not very pressure sensitive (170). Although this might be expected if the flow were primarily osmotically driven into the uveal vessels, this would not be the expected characteristic of a trans-scleral flow. Each of these considerations argue against trans-scleral flow, but are consistent with osmotic adsorption of the unconventional aqueous outflow by the choroidal circulation (123).

SUMMARY AND OPEN PROBLEMS

From this brief summary it is clear that there is a great deal of interesting biomechanics in the eye. We are far from understanding all the relevant biomechanics in this understudied field, and hence we close with a list of open problems to tempt researchers.

■ Why does presbyopia occur? There have been no biomechanical modeling studies that account for all of the physiological observations mentioned in Accommodation and Presbyopia (above) and attempt to comprehensively evaluate the mechanisms underlying presbyopia. More generally, fundamental studies about the biomechanics of accommodation are also needed.

■ How is outflow resistance generated in the normal eye, and what goes wrong to increase this resistance in most forms of glaucoma?

■ How does elevated IOP damage the optic nerve and lead to blindness in glaucoma?

■ What are the biomechanics of myopia?

■ How can we determine microscale material properties and corneal stress field noninvasively, in vivo? If this can be accomplished, then the biomechanicist might provide input for refractive corneal surgery on a case-by-case basis.

■ How is the hydration of the cornea controlled? No control signal has been identified to date, yet corneas maintain their hydration in a relatively tight range. Recently, Ruberti & Klyce (171) demonstrated that 5% changes in NaCl concentration induced compensatory changes in endothelial pump rate, suggesting a possible homeostatic response triggered by NaCl.

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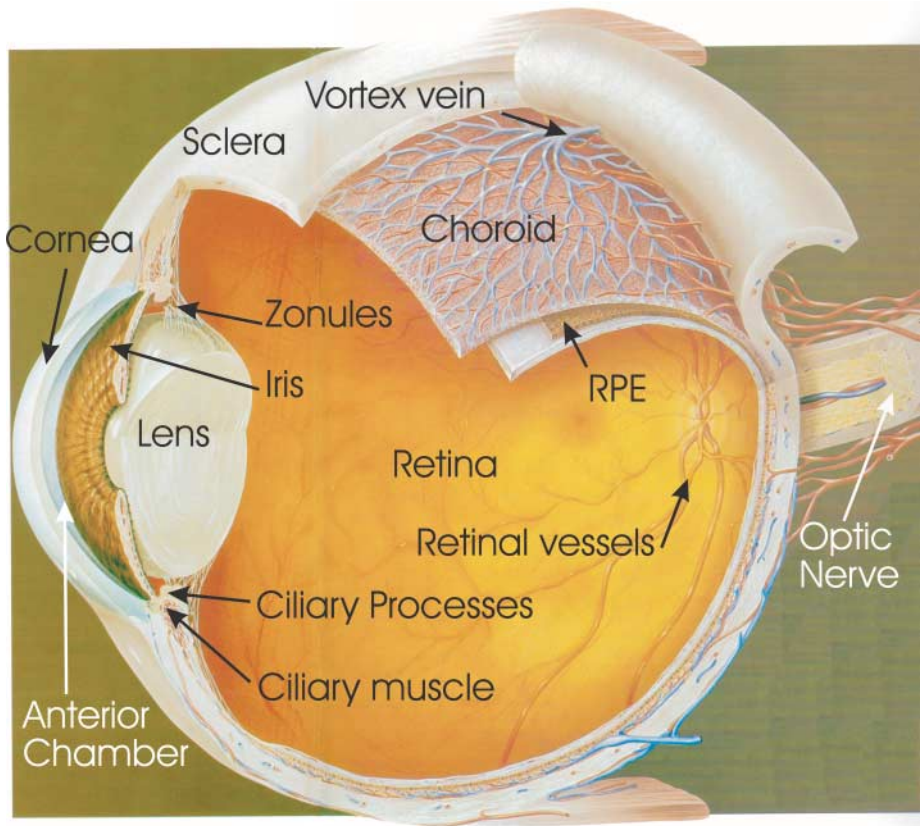172. Ritch R, Shields MB, Krupin T, eds. 1989. *The Glaucomas*. St. Louis, MO: C.V. Mosbey Co.

Figure 1   Overview of ocular anatomy, with several key ocular components labelled. Modified from (2).
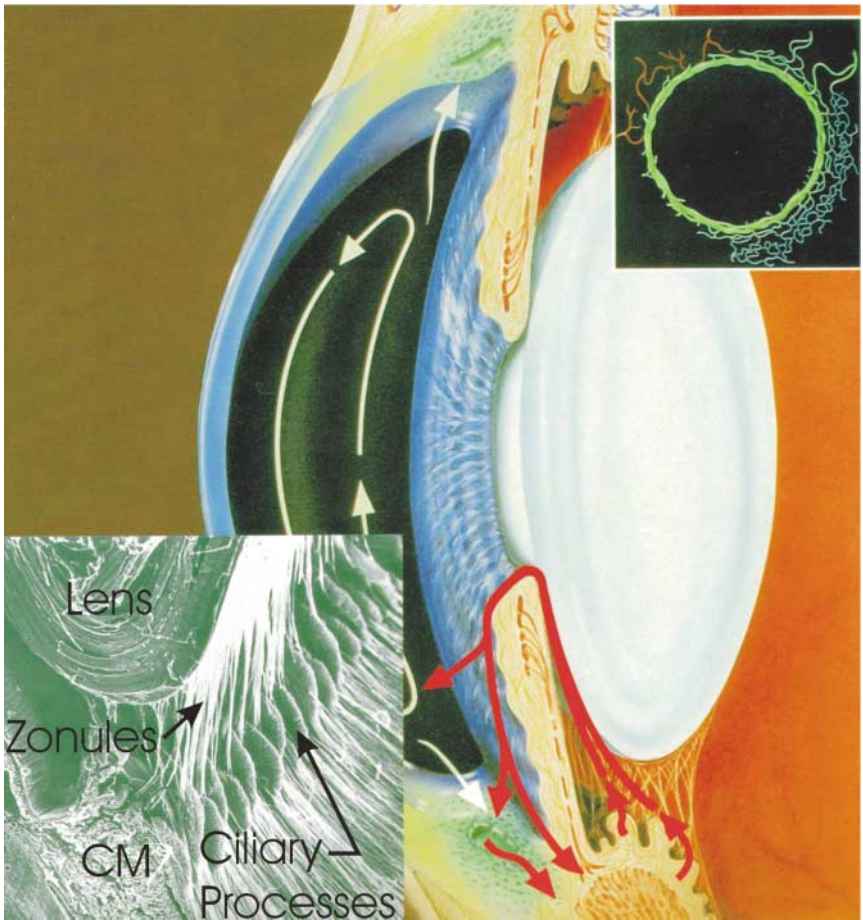
Figure 4   View of anterior segment of eye, showing site of production of aqueous humor (ciliary processes) and drainage routes (*red arrows*). The white arrows in the anterior chamber show thermal convection patterns. The lower left inset is a scanning electron micrograph of the zonular apparatus (CM = ciliary muscle). The inset at upper right shows Schlemm's canal (*green*) as seen face-on. Green vessels anatomising with Schlemm's canal are collector channels; blue vessels are aqueous veins; red vessels are arterioles. Modified from (2).